

# University of Asia Pacific

## Department of Civil Engineering

### Final Examination Fall 2012

#### Program: B.Sc. Engineering (Civil)

Course title: Open Channel Flow

Course code: CE 361

Time: 3 hours

Total Marks: 100

Answer any **FIVE** out of **SEVEN** questions. Each question has **20** marks. The figures in the right margin indicate full marks.

#### 1.

- a) Define the following terms: 6  
a. Manning's coefficient   b. Normal depth   c. Chezy's C
- b) State the characteristics of uniform flow in an open channel. 3
- c) Water flows at a velocity of 1 m/s in an open channel under uniform flow condition. The longitudinal slope of the channel is 0.0016 and  $n=0.02$ . Compute the normal depth of flow when the channel is trapezoidal with  $b=6$  m and  $s=2$ . 5
- d) A rectangular channel has a bottom width of 5 m and Manning's coefficient  $n=0.025$ . The channel lies on a slope of 1 in 1000. Determine the critical slope when discharge is  $20 \text{ m}^3/\text{s}$ . 6

#### 2.

- a) An open channel with concrete lining ( $d_{50}=1.5\text{mm}$ ) is laid on a slope of 0.1%. The channel is trapezoidal with bottom width of 3.5m and side slope  $s=2$ . If the depth of flow is 2.1m, find the uniform flow  $Q$ , Chezy's coefficient 'C' and friction factor 'f'. 6
- b) Differentiate between 'section factor' and 'conveyance' for uniform flow in an open channel. 4
- c) An unlined irrigation channel ( $n=0.025$ ) is trapezoidal and has a bottom width of 7m, side slopes of 1:1, and depth of flow of 2m. The longitudinal slope of the canal is 0.0005. It is proposed to line the canal with concrete ( $n=0.013$ ). Compute the discharge when only sides are lined with concrete. 6
- d) List the factors that affect the Manning's coefficient 'n'. 4

3.

- a) What is a lined channel? What are the reasons for lining a channel? 5
- b) A lined channel ( $n=0.015$ ) is to be laid on a slope of 1 in 2500. The side slope of the channel is to be maintained at 1.5:1. Determine the dimensions of a trapezoidal section with rounded corners to carry a discharge of  $m^3/s$  when the maximum permissible velocity is 2 m/s. 7
- c) Define a best hydraulic section. Why do you think it is not always possible to find a best hydraulic section? 4
- d) Show that the best hydraulic triangular section is one half of a square. 4

4.

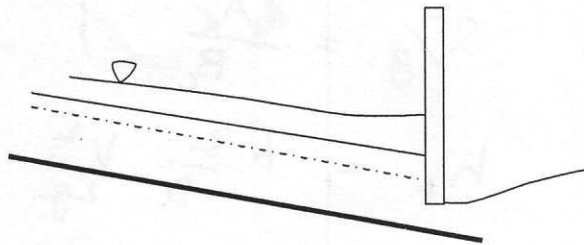
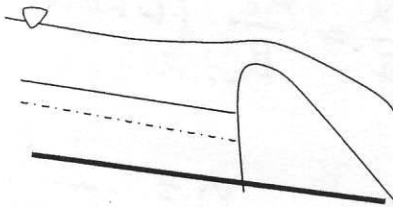
- a) Define the following terms: 6
- a. Maximum permissible velocity
  - b. Non-silting velocity
  - c. Freeboard
- b) A trapezoidal channel is to be laid on a slope of 1 in 1000 and carry a discharge of  $20 m^3/s$ . It is to be excavated in earth containing slightly rounded coarse non-cohesive particles with  $d_{75} = 3$  cm and  $n = 0.025$ . Determine the section dimensions of the channel using the method by Lane. 6
- c) What is 'angle of repose'? Why critical shear stress is important for channel design? 4
- d) A horizontal trapezoidal channel having bottom width  $b = 5.5$  m,  $s = 2$  carries a discharge of  $130 m^3/s$  at a depth of 1.1 m. Compute the downstream depth that will form a hydraulic jump. Find the energy loss in the hydraulic jump. 4

5.

- a) Write down the characteristics of 'Gradually Varied flow'. 4
- b) Derive the following equation for gradually varied flow in an open prismatic channel. State the assumptions you made to derive the equation. 6
- $$dy/dx = (S_o - S_f)/(1 - Fr^2)$$
- c) In terms of the above equation, how do you explain 'backwater curve' and "drawdown curve"? 3
- d) A rectangular channel with  $b = 4$  m, and  $n = 0.015$  carries a discharge of  $18 m^3/s$ . Identify the flow profiles produced in the channel for the following changes in the channel bottom slope:  
 $S_o = 0.004$  to  $S_o = 0.009$  7

6.

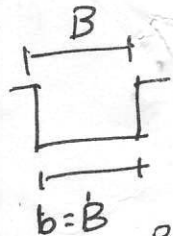
- a) Sketch the possible water surface profiles in the following cases: 6
- a. Horizontal slope – Mild slope --- Critical slope
  - b. Steep slope --- Critical slope --- Mild slope
  - c. Mild slope --- Milder slope – Steep slope
- b) A trapezoidal channel having  $b=5\text{m}$ ,  $s=2$ ,  $n=0.02$  and  $S_0=0.002$  carries a discharge of  $48.67\text{ m}^3/\text{s}$ . A dam constructed across the channel raises the water level to a depth of  $5\text{ m}$  immediately upstream of it. How far upstream or downstream from the dam will the depth be  $4.75\text{m}$ ?  
Use the direct step method. 6
- c) Define 'tailwater depth'. Using sketches, describe the importance of 'tailwater depth' in hydraulic jump with respect to downstream water depth  $y_2$ . 5
- d) What do you understand by 'control section'? Indicate control sections in the following figures. 3



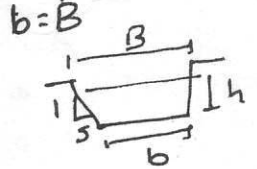
7.

- a) When does a hydraulic jump take place in an open channel? Write down some of the practical applications of a hydraulic jump. 4
- b) The depth and velocity at the foot of an overflow spillway are  $0.5\text{m}$  and  $15.50\text{m/s}$  respectively. What tailwater depth is needed to form a hydraulic jump? If a jump is formed, determine the type of jump, the height of jump, the length of jump, and the energy loss in the jump as a percentage of the initial energy. 6
- c) A rectangular channel is  $1.5\text{ m}$  wide, and inclined at an angle of  $4.0$  degree with the horizontal. The channel carries a discharge of  $0.75\text{ m}^3/\text{s}$  at a vertical depth ( $h_1$ ) of  $0.05\text{ m}$ . If a hydraulic jump occurs in this channel, compute the sequent depth, length of jump and height of jump. 6
- d) State the differences between steady jump, weak jump and strong jump. 4

1.  $A = bh$  ;  $P = b + 2h$  ;  $B = b$



2.  $A = (b + sh)h$  ;  $P = ~~b~~ b + 2\sqrt{1+s^2}h$



$B = b + 2sh$  ;

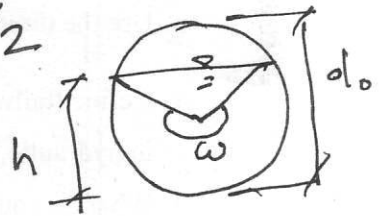
3.  $A = sh^2$  ;  $P = (2\sqrt{1+s^2})h$  ;  $B = 2sh$



4.  $h = d_0 [1 - \cos(\frac{\omega}{2})] / 2$

$A = (\omega - \sin \omega) d_0^2 / 8$

$P = \omega d_0 / 2$



5.  $Q^2/g = \frac{A_c^3}{B_c}$  ;  $\frac{\alpha Q}{g} = \frac{A_c^3}{B_c}$  (when  $d \neq 1.0$ )

6.  $h_f = f \frac{L}{D} \frac{V^2}{2g}$  ;  $n = \frac{d^{1/6} s_0}{21.1}$

7.  $Re = \frac{VD}{\nu}$  (d in meters)

8.  $C = \sqrt{8g/f}$

9.  $C = \frac{1}{n} R^{1/6}$

10.  $\tau_0 = \gamma R S_0$

11.  $u_* = \sqrt{\frac{\tau_0}{\rho}} = \sqrt{g R S_0}$

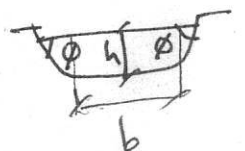
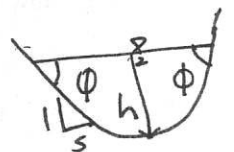
12.  $S_{ov} = \frac{11.6 \nu}{u_*^2}$

13.  $A = h^2 (\phi + \cot \phi)$

$P = 2h (\phi + \cot \phi)$

$A = bh + h^2 (\phi + \cot \phi)$

14.  $P = b + 2h (\phi + \cot \phi)$



15. Best Hydraulic Sections

	A	P	B	D
Rectangle	$2h^2$	$4h$	$2h$	$h$
Triangle	$h^2$	$2\sqrt{2}h$	$\frac{\sqrt{2}b^2}{2h}$	$h/2$
Trapezoid	$\sqrt{3}h^2$	$2\sqrt{3}h$	$4\sqrt{3}h/3$	$3h/4$
Circle	$\pi h^2/2$	$\pi h$	$2h$	$\pi h/4$

16. For a trapezoidal ~~section~~ best hydraulic section:

$$A = (2\sqrt{1+s^2} - s)h^2$$

$$b = 2(\sqrt{1+s^2} - s)h$$

$$P = 2h(\sqrt{1+s^2} * 2 - s)$$

17. Erodeable channel:

$$\Rightarrow \tau_0 = \gamma R s_0.$$

$$\Rightarrow K = \frac{\tau_s}{\tau_b} = \sqrt{1 - \frac{\sin^2 \phi}{\sin^2 \psi}}$$

where  
 $\psi$  = angle of repose  
 $\phi$  = side slope angle.

$\Rightarrow$  permissible shear stress =  $0.4 d_{75}$   
 ( $d_{75}$  in inches)

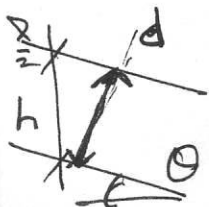
$$\Rightarrow \bar{S}F = (SF_1 + SF_2) / 2$$

$$\Rightarrow x_2 = x_1 + \frac{E_2 - E_1}{s_0 - \bar{S}F}$$

18.  $\frac{y_2}{y_1} = \frac{1}{2} (\sqrt{1 + 2G^2} - 1)$

19.  $G^2 = K_1^2 Fr_1^2$  where  $K_1 = 10$

20.  $h = d \cos \theta$



$0.027 \theta$

( $\theta$  is in deg)



21.  $\frac{y_2}{y_1} = \frac{1}{2} \left( \sqrt{1 + 8Fr_1^2} - 1 \right)$

or,  $\frac{y_1}{y_2} = \frac{1}{2} \left( \sqrt{1 + 8Fr_2^2} - 1 \right)$

22.  $h_L = \frac{(y_2 - y_1)^3}{4y_1 y_2}$

23.  $\frac{L_j'}{y_1} = 9.75 (Fr_1 - 1)^{1.01}$

24.  $\frac{E_2}{E_1} = \frac{(1 + 8Fr_1^2)^{3/2} - 4Fr_1^2 + 1}{8Fr_1^2 (2 + Fr_1^2)}$

25.  $\frac{h_3 \text{ (submerged)}}{h_t \text{ (full water)}} = \left[ 1 + 2Fr_1^2 \left( 1 - \frac{h_t}{h_g} \right) \right]^{1/2}$

26.  $Fr^2 = \frac{Q^2 B}{g A^3}$

$Fr = 1$  (critical flow condition)

27.  $\bar{z}$  for different sections

Rectangle -  $h/2$

triangle -  $h/3$

trapezoid -  $\frac{h}{6} \left( \frac{3b + 2sh}{b + sh} \right)$

28. Specific force  $F = \frac{Q^2}{gA} + \bar{z} A$

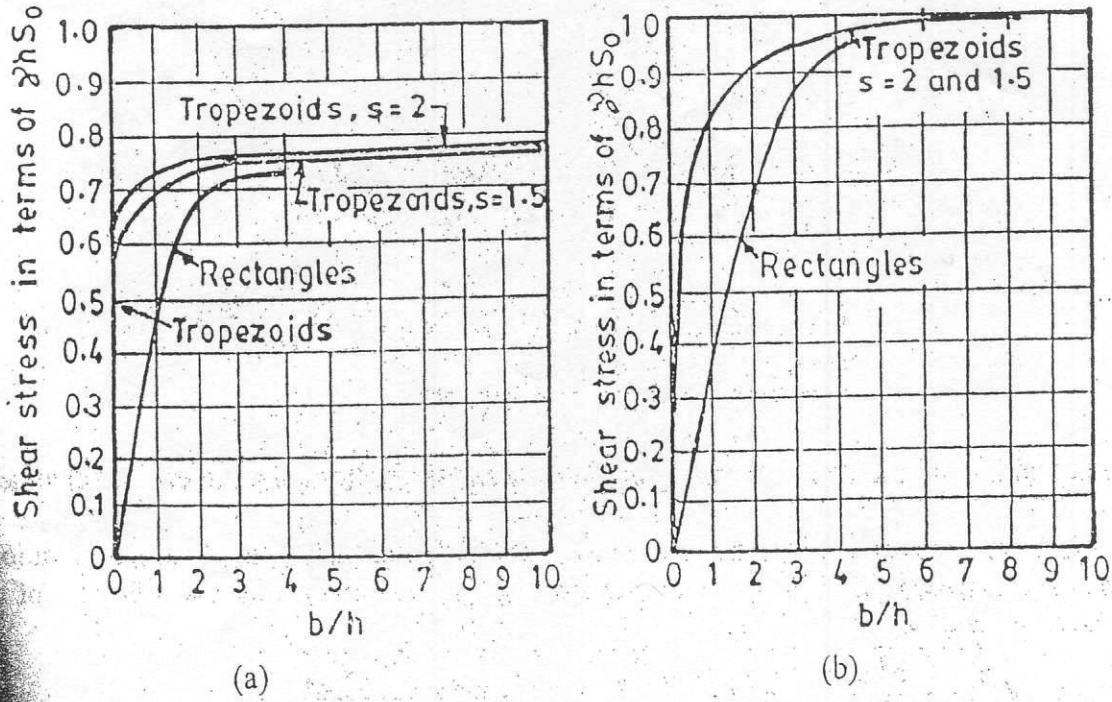


Fig. 5. 4 Maximum shear stresses on (a) sides and (b) bottom of trapezoidal channels

Stress Ratio

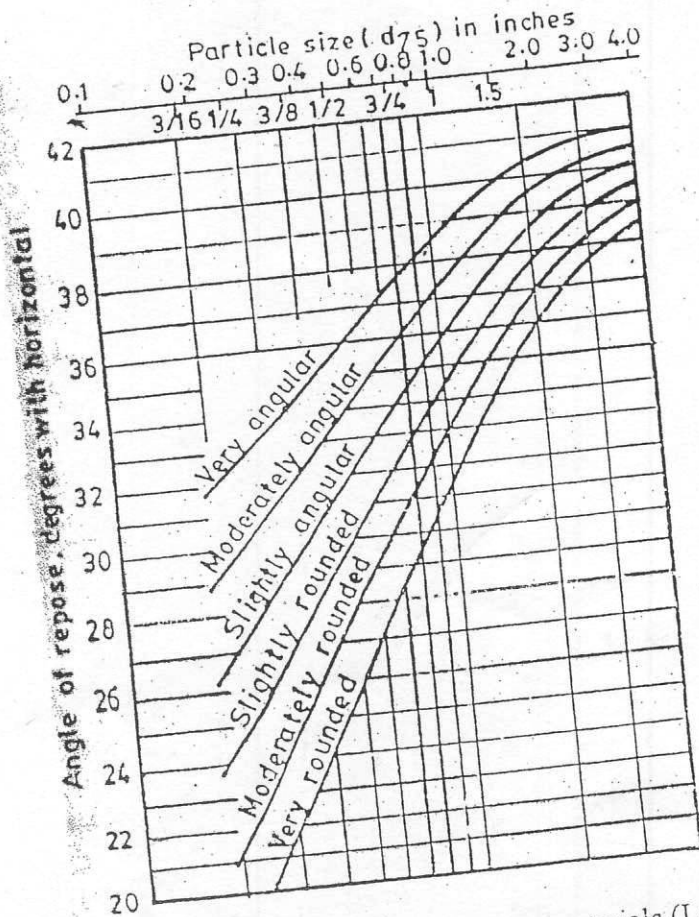


Fig. 5. 6 Angle of repose of non-cohesive materials (Lane, 1955)

and the size of the sediment particle. The